

Bonds

① Introduction

② Bond Alphabet Soup and the Basic Price Formula

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2 Bond Alphabet Soup and the Basic Price Formula

Vocabulary

Assignment: Read thoroughly Section 6.1

- **Bonds** are financial products that are issued by and can be purchased from a government bureau or a financial company that guarantees future payments
- The time of purchase of the bond is called the **issue date**
- The life of a bond is **finite**; there is a **maturity date** (or **redemption date**) when the last payment occurs
- The maturity date is fixed, but there may be a stipulation that the bond may be **called** earlier and the redemption amount must be given to the holder of the bond; such bonds are referred to as **callable bonds**
- The **term** of the bond is the interval between the issue date and the maturity date (or the length of that interval, depending on the context)

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More vocabulary

- **Zero-coupon bonds** (or **pure discount bonds**) have only a single payment at the fixed maturity date]
- The bonds that have intermediate payments are called **coupon bonds**
- The time periods between two consecutive payments that occur before maturity are referred to as **coupon periods**
- The **indenture** is the legal document (contract) that specifies all of the above

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What's printed on the bond?

- F ... the **face** (or **par**) **value** of a bond
- The par value is used to calculate **the size of the coupon payments**
- Assume that m is the number of coupons issued during a year and that α is the nominal rate convertible m times per year; then, $r = \alpha/m$ is the effective rate per coupon period
- Then, the amount of a coupon payment equals

$$Fr = \frac{F\alpha}{m}$$

- *Caveat:* **Both** α and r can be referred to as **coupon rates**

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Modified coupon rate

- n ... the number of coupon periods in the term of a bond
- So, if a bond is an N -year bond, then $Nm = n$
- C ... the redemption amount
- IF $C = F$, then the bond is called a par-value bond (or redeemable at par)
- *Convention:* If it is not specified otherwise, one should assume that $F = C$
- g ... the modified coupon rate, i.e.,

$$g := \frac{Fr}{C}$$

- Note that the coupon amount equals $Fr = Cg$

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Investor's effective yield rate

- i ... the investor's effective yield rate **per year**
- j ... the investor's effective yield rate **per coupon period**
- v_j ... the discount factor per coupon period, i.e.,

$$v_j = \frac{1}{1+j}$$

- G ... the **base amount**, i.e.,

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Basic price formula

- K ... the value of the redemption amount at the issue date, i.e.,

$$K = Cv_j^n$$

- P ... the price paid for the bond by the investor if j is the desired yield rate per period, i.e.,

$$P = (Fr) \cdot a_{\overline{n}|j} + Cv_j^n = (Fr) \cdot a_{\overline{n}|j} + K$$

- All the notation is collected in Table 6.2.4 in the book - keep it handy as you do the problems until you get used to all the vocabulary and notation ...
- *Assignment:* Do **all** the examples in Section 6.2.

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