Bond Amortization Schedule

- The bonds can be seen as loans that the holder of the bond gives to the issuer of the bond; the coupon payments and the redemption payment are there to repay this loan
- The coupon period plays the role of the payment period we are familiar with from the context of amortized loans
- The investor's effective yield rate per coupon period j stands for the per payment period interest rate in the set-up for loan repayment
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- B_t, t ∈ [0, n], denotes the balance of debt at time t immediately after any time t coupon payment, but before redemption payment, i.e., the book value of the bond at time t
- Caveat: B_t is calculated using the investor's yield rate j and does
 not take into account market forces (e.g., the prices of bonds on the
 secondary market)
- In particular,

$$B_0 = P$$
 and $B_n = C$

• I_t ... the interest due at time of the t^{th} coupon, i.e.,

$$I_t = jB_{t-1}, \quad t = 1, 2, \dots, n$$

$$P_t = B_{t-1} - B_t$$
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• From the basic price formula:

$$B_t = F r a_{\overline{n-t}|j} + C v_j^{n-t}$$
 $t = 0, 1, 2, \dots, n$

From the premium-discount formula

$$B_t = C(g - j)a_{\overline{n-t}|j} + C$$
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$$I_t = jB_{t-1} = Cg - C(g - j)v_j^{n-t+1}$$

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At a premium:

If a bond sells at a premium, then g>j and P_t is positive for every t. So, a portion of each coupon compensates the investor for the premium initially paid for the bond and the rest goes towards the interest payment on that premium.

At a discount:

If a bond sells at a discount, then g < j and P_t is negative for every t. Thus, not even the interest due on the balance can be covered by the coupon payments meaning that the remainder of the interest due is added onto the outstanding loan balance which increases as time goes by

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- The process of finding the values of B_t is called writing down the bond
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Odds and Ends

- Figure 6.5.11 contains an amortization table for a bond with level coupons, with all the entries in the table described as functions of the inputs of the bond
- In any case, the following recursion formula holds:

$$B_t = (1+j)B_{t-1} - Cg$$

Assignment: ALL examples from Section 6.5.

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