

Please, provide your complete solution to the following problems:

**Problem 2.1.** (5 points) Provide your complete solution to **Problem 1.7.8** from the textbook.

**Problem 2.2.** (6 points) Assume our usual notation. The accumulation of interest in an account is governed by the following:

a nominal interest rate convertible semiannually of 9% for the first 3 years,

a nominal discount rate convertible quarterly of 10% for the following 2 years,

$d = 7\%$  for the next 2 years,

$i = 12\%$  thereafter.

Roger makes an initial deposit of \$100. He makes no subsequent deposits or withdrawals, and liquidates his account after 10 years. Calculate the amount he is able to withdraw at that time.

**Problem 2.3.** (9 points) *Source: SoA Exam FM, May 1988, Problem #3.*

Two funds, A and B, start with the same amount.

Fund A grows at an annual interest rate  $i > 0$  for  $n$  years, and at an annual interest rate  $j > 0$  for the next  $n$  years. Fund B grows at an annual interest rate  $k > 0$  for  $2n$  years.

Fund A equals 1.5 times fund B after  $n$  years. The amount in the two funds are equal after  $2n$  years. Which of the following are true?

- i.  $j < k < i$
- ii.  $k < \frac{i+j}{2}$
- iii.  $j = k \left(\frac{2}{3}\right)^{1/n}$

**Problem 2.4.** (5 points) *Source: SoA Exam FM/2, November 1988, Problem #4.*

John borrows \$1,000 from Jane at an annual effective interest rate  $i$ . He agrees to pay back \$1,000 after six years and \$1,366.87 after another six years.

Three years after his first payment, John repays the outstanding balance. What is the amount of John's second payment?

**Problem 2.5.** (10 points) *Source: SoA Exam FM/2, May 1989, Problem #1.*

Investment X for \$100,000 is invested at a nominal rate of interest  $j$  convertible semiannually. After four years, it accumulates to \$214,358.88.

Investment Y for \$100,000 is invested at a nominal rate of interest  $k$  convertible quarterly. After two years, it accumulates to \$232,305.73.

Investment Z for \$100,000 is invested at an annual effective rate of interest equal to  $j$  in year one and an annual effective rate of discount equal to  $k$  in year two. Calculate the value of the investment Z in two years.

**Problem 2.6.** (5 points) *Source: SoA Exam FM/2, May 2003, Problem #50.*

Jeff deposits 10 into a fund and 20 fifteen years later. Interest is credited at a nominal discount rate of  $d$  compounded quarterly for the first 10 years and at a nominal interest rate of 6% compounded semiannually thereafter. The accumulated balance in the fund at the end of thirty years is 100. Calculate  $d$ .

**Problem 2.7.** (5 points) *Source: SoA Exam FM/2, May 1998, Problem #2.*

John invests 1000 in a fund which earns interest during the first year at a nominal rate of  $\kappa$  convertible quarterly. During the second year, the fund earns interest at a nominal discount rate of  $\kappa$  convertible quarterly. At the end of the second year, the fund has accumulated to 1173.54. Calculate  $\kappa$ .

Please, provide your final answer only for the following problems.

**Problem 2.8.** (5 pts) Roger makes an initial investment of \$100,000.

In return, he gets cash flows of \$40,000 at the end of each of years 2, 3 and 4. The cash flows can be reinvested at 4.0% per annum effective.

If the rate of interest at which the investment is to be valued is 5.0%, let  $P$  denote the net present value of this investment today. Then,

- (a)  $P < 0$
- (b)  $0 \leq P < 700$
- (c)  $700 \leq P < 1400$
- (d)  $1400 \leq P < 1600$
- (e) None of the above.