M346 (55820) Applied Linear Algebra, Spring 2012 Course syllabus (last revised: 05/07/2012)

Instructor: Ravi Srinivasan Email: rav@math.utexas.edu Office: RLM 11.164 Office hours: W 1:30-4:00 (will change depending on HW due dates)

Lecture: MWF 12-1, RLM 5.124 Class website: http://www.ma.utexas.edu/users/rav/M346/

Required texts:
(1) ``Applied Linear Algebra: The Decoupling Principle (2nd ed.)'' by L. Sadun (ISBN
0821844415);
(2) ``Linear Algebra Done Wrong'' by S. Treil
(http://www.math.brown.edu/~treil/papers/LADW/book.pdf)

Prerequisites and degree relevance: A grade of C or better in M341 (or M311) or M340L, or consent of the instructor.

Course description and content:

This is an advanced undergraduate course on linear algebra directed at students in the natural and social sciences and at engineering students. The emphasis in this course is both on theoretical considerations (with rigorous proofs of results) and on problem solving. Topics include vector spaces, linear transformations and matrix representation, spectral theory (both discrete and continuous), diagonalization of linear operators, inner products and duality, Hermitian (i.e., self-adjoint) and unitary operators, the Fourier transform, and applications to differential equations, probability theory, and network analysis.

Notice:

The University of Texas provides appropriate academic accommodations for qualified students with disabilities. For more information, contact the Office of the Dean of Students at 471-6259, 471-6441 TTY. If you plan on using accommodations, you need to notify your instructors early in the semester.

Important dates: Fri., Jan. 20, 2012 -- Last day of official add/drop period Wed., Feb. 01, 2012 -- Last day to drop a course for possible refund (can only Q-drop after this date) Mon., Apr. 02, 2012 -- Last day to withdraw/drop a class with Dean's approval, change status to or from a pass/fail basis

Grading:

Grades will be determined from weekly homework/quizzes, midterms, and the final exam (see below). Course grades will be computed on a +/- basis according to a scheme at least as generous as this (rounded to the closest integer):

A : 92-100

- A-: 90-91
- B+: 88-89
- B : 82-87
- B-: 80-81
- C+: 78-79
- C : 72-77
- C-: 70-71
- D+: 68-69
- D : 62-67
- D-: 60-61
- F : < 60

1. Homework: 20%

Homework assignments will be posted online every week on the class website, approximately one week before it is due. Assignments will be due almost every Wednesday in lecture, and late homework will *not* be accepted. The purpose of the HW is to learn the material. You are encouraged to discuss and work together on these problems, including during office hours. Learn to correctly and consistently derive the answer (without a calculator) in order to better prepare for exams. Do not restrict yourself to HW problems, but use them as a basis for trying questions from the book as well. Only a select set of questions will be graded each week, and you will get a minimal amount of credit simply for handing in your complete HW solutions.

The *three* lowest HW grades will be dropped to allow for missed lectures, illness, emergencies, etc. Even if you do not hand in HW solutions, make sure to complete the assigned problems in order to prepare for exams.

2. Midterm exams: 50% There will be three 50-minute midterms given in regular class times on the following dates (subject to change):

- 2a. Midterm #1: 10% Monday, Feb. 13, 2012
- 2b. Midterm #2 (not comprehensive): 20%
 Friday, Mar. 23, 2012
- 2c. Midterm #3 (not comprehensive): 20%
 Wednesday, Apr. 25, 2012

Final exam (comprehensive): 30%
 Saturday, May 12, 7-10pm (officially assigned date/time), RLM 5.124

Exam policy:

A valid photo ID must be available to be checked at all exams. Calculators, books, and notes are not permitted during quizzes, midterms, and the final exam.

Make-up exams **will not** be given so please remember the appropriate exam dates. In extraordinary circumstances ONLY, the final exam score will compensate for a missing midterm exam. This includes illness, observance of a religious holiday, or a university-related absence *with two weeks advance notice.* Proper documentation (such as a doctor's note) is required in all cases.

Some tips:

- Ask questions: In lecture, office hours, and by e-mail. Don't be shy--if you have a question it's likely someone else does as well. Class participation makes lectures more interesting and fun for both you and me.

- Do the homework: No one can learn mathematics without working examples themselves. The most important driver of success in virtually every math course is doing practice exercises carefully and completely.

- Read the text: To get the most benefit from the lectures and problem sessions, you should read relevant sections of the text as they are covered in class. The supplementary texts listed can also be useful references at particular times in the course.

- Come to office hours: Office hours offer valuable opportunities to reinforce concepts, clarify confusing issues, work more examples, and get individualized feedback.

- Study together: You are encouraged to study together with your peers enrolled in the class. Get to know your classmates, and make arrangements to share notes in case you miss class due to illness.

- Learn to work problems without a calculator: You may use a calculator on homework problems but not during quizzes or exams. In any case, a calculator will not be useful for the vast majority of problems encountered during the semester.

- Be honest: Any academic dishonesty will be severely penalized.

Tentative course calendar (subject to change):

====== PART I: Finite-dimensional linear operators =======

--Week 01--Topics: Introduction (1.1), vector spaces (2.1), matrix operations (Appendix A) W 01/18 First lecture F 01/20

--Week 02--

Topics: Basis and dimension (2.2), properties and change of basis (2.3-2.4), linear transformations and matrix representation (3.1-3.2) M 01/23 W 01/25 HW1 due F 01/27 --Week 03--Topics: Basis and operators (3.3), subspaces (3.5) M 01/30 W 02/01 HW2 due F 02/03 ====== PART II: Diagonalization and applications ======= --Week 04--Topics: Eigenvalues and eigenvectors (4.1-4.2), characteristic polynomials (4.3) M 02/06 W 02/08 HW3 due F 02/10 --Week 05--Topics: Complex eigenvalues (4.4), diagonalizability (4.5) **MIDTERM #1** (on Part I) M 02/13 W 02/15 F 02/17 HW4 due --Week 06--Topics: Jordan canonical form (4.9), trace and determinant (4.6), first-order difference equations (5.1), matrix exponentials (4.7) M 02/20 W 02/22 F 02/24 HW5 due --Week 07--Topics: Systems of first-order ODE (5.2), stability and asymptotic behavior (5.5), Markov chains (5.6) M 02/27 W 02/29 F 03/02 HW6 due --Week 08--Topics: Markov chains (cont'd), applications in network science M 03/05 W 03/07 F 03/09 HW7 due --Spring break--

====== PART III: Inner-product spaces, self-adjoint operators and spectrum ======= --Week 09--Topics: Inner-product spaces (6.1-6.2), duality (6.3) M 03/19 03/21 HW8 due W F 03/23 **MIDTERM #2** (on Part II) --Week 10--Topics: Orthogonalization and Gram-Schmidt procedure (6.4-6.5), projections (6.6), least-squares (6.7) M 03/26 W 03/28 03/30 HW9 due F --Week 11--Topics: Adjoints (7.1), self-adjoint operators (7.2), normal operators M 04/02 W 04/04 F 04/06 HW10 due --Week 12--Topics: Unitary and orthogonal operators (7.4), positive operators, singular value decomposition M 04/09 W 04/11 F 04/13 HW11 due ====== PART IV: Infinite-dimensional self-adjoint operators, distributions and Fourier analysis ====== --Week 13--Topics: Applications of SVD, infinite-dimensional spaces (3.4, 6.8), Fourier series (6.9) M 04/16 W 04/18 F 04/20 HW12 due --Week 14--Topics: Fourier series (cont'd) (6.9, 8.5, 8.7) M 04/23 W 04/25 **MIDTERM #3** (on Part III) F 04/27 --Week 15--Topics: Continuous spectrum and generalized eigenfunctions (9.1), introduction to distributions (9.2-9.3), Fourier transform (10.1) M 04/30 W 05/02

F 05/04 HW13 due, last lecture

--Finals week--Sa 05/12 **FINAL EXAM** 7pm-10pm, RLM 5.124