

Algebraic Topology

Homework 11: Due Wednesday, November 17

Problem 1. Compute the homology of the Lens space $L(p, q)$.

Problem 2. Let X be a torus with two disks glued in, exactly as in the midterm. Compute the homology of X .

Problem 3. Page 172, problem 5.2.

Problem 4. Page 172, problem 5.4.

Problem 5. Page 175, problem 6.2.

Problem 6. Suppose that $A \subset B \subset X$. Show that there is a long exact sequence $\rightarrow H_k(B, A) \rightarrow H_k(X, A) \rightarrow H_k(X, B) \rightarrow H_{k-1}(B, A) \rightarrow \cdots$. What are the maps in this sequence? [This sequence is called the long exact sequence of the triple (X, B, A) . When A is the empty set, it becomes the usual long exact sequence of the pair (X, B) .]