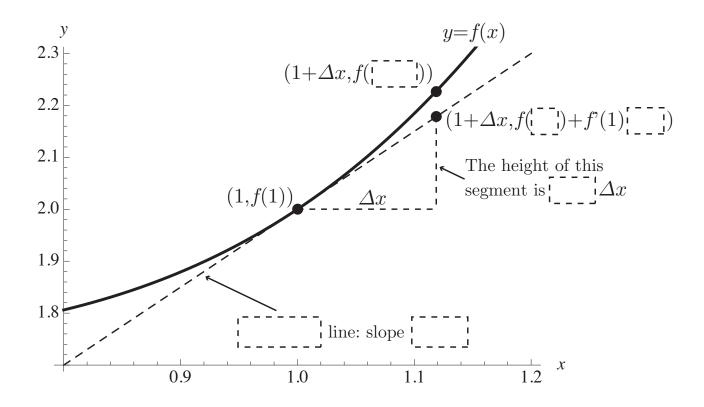
September 30, 2014 Worksheet 8: differentiation rules; the microscope equation

1. (Geometric interpretation of the Microscope Equation.) The graph of a function f(x) appears below (solid), along with the graph of the line tangent to f(x) at the point (1, f(1)) (dashed). (Note that the axes here do NOT intersect at (0,0).)

Fill in the dashed rectangles (there are seven of them) on the picture below, by inserting exactly one of the following terms in each rectangle.

1 Δx 1+ Δx f'(1) f(1)+f'(1)\Delta x tangent

Note: All terms will be used, some perhaps more than once.



As the picture illustrates, for Δx small,

 $f(1 + \Delta x) \approx$

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2. (The Chain Rule and the Microscope Equation.)

(a) Find
$$\frac{d}{dx} \left[\sqrt{3 + \sqrt{x}} \right]$$
.

(b) Write down the microscope equation for $f(x) = \sqrt{3 + \sqrt{x}}$ at x = 1.

(c) Use your answer to part (b) above to estimate $\sqrt{3 + \sqrt{1.04}}$.

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3. (Differentiation rules.) Fill in each blank on the right hand side with the name of the rule that is being used there. (At most one rule is being used per line. In "real life," you might want to combine some steps.) If *no* rules are being used, then write "none."

The first blank has been filled in for you.